

February 3, 2017

Math 124b

Name Key

1. (5 pts) Consider the function,

$$y = \sqrt{6 - x^2}$$

Find the domain of this function. Determine the  $x$  and  $y$ -intercepts. Sketch a graph of the function.

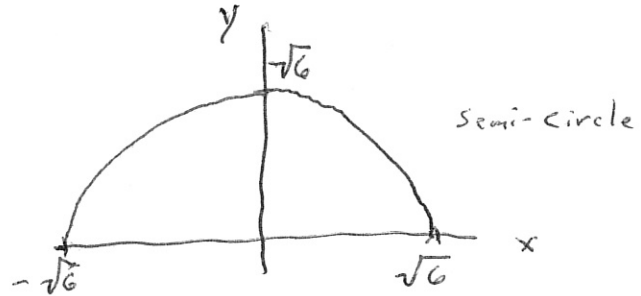
$$-2.4495 \leq x \leq 2.4495$$

Domain:  $-\sqrt{6} \leq x \leq \sqrt{6}$

$x$ -intercepts  $\pm \sqrt{6}$

$y$ -intercept  $\sqrt{6}$

Sketch of Graph:



2. (7 pts) Consider the function,

$$y = \frac{8 + 3x}{x - 4}$$

find the domain. Find all  $x$  and  $y$ -intercepts. Determine any horizontal or vertical asymptotes. (If no asymptote exists, then write "NONE.") Sketch the graph.

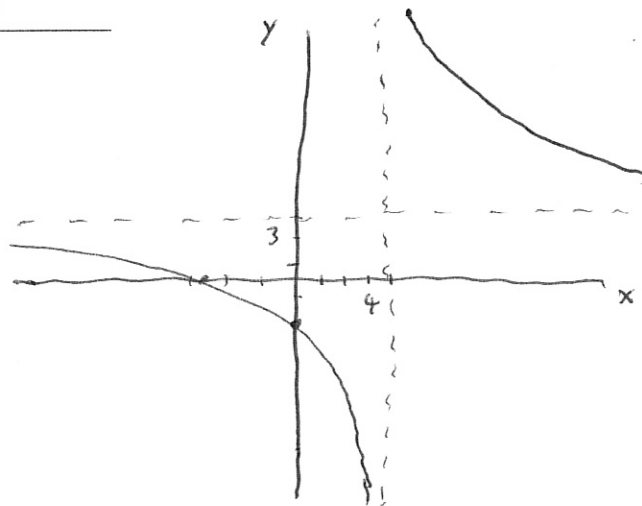
Domain:  $x \neq 4$

$x$ -intercept  $-\frac{8}{3}$  and  $y$ -intercept  $-2$

Vertical Asymptote:  $x = 4$

Horizontal Asymptote:  $y = 3$

GRAPH:



2. (8 pts) The Lambert-Beer law for absorbance of light by a spectrophotometer is a linear relationship, which can have the form,

$$A = mc,$$

where  $c$  is the concentration of the sample,  $A$  is absorbance, and  $m$  is the slope that must be determined from standards.

a. Below are data collected on samples from a collection of acid standards using an acid indicator.

$c$ (mM)	1	2	5
$A$	1.7	3.2	8.3

Write all the square errors. Write a quadratic function  $J(m)$  that measures the sum of squares error based on the standards above for the line fitting the data. Find the vertex of this quadratic function.

$$e_1^2 = \frac{(1.7 - m)^2}{1} = 2.89 - 3.4m + m^2$$

$$e_2^2 = \frac{(3.2 - 2m)^2}{1} = 10.24 - 12.8m + 4m^2$$

$$e_3^2 = \frac{(8.3 - 5m)^2}{1} = 68.89 - 83.0m + 25m^2$$

$$J(m) = 30 m^2 + 99.2 m + 82.02$$

$$\text{The vertex location } m_v = 1.6533$$

b. The vertex gives the value of the best slope  $m$ . Use this model (with the best value of  $m$ ) to determine the concentration of an unknown sample with an absorbance of  $A = 2.5$ .

$$c = 1.5121$$

$$c = \frac{A}{m} = \frac{2.5}{1.6533}$$