Spring 2008 Math 531

Computer Problem

1. a. Consider a one-dimensional rod that is insulated along its edges. Assume that it has a length of 10 cm. The rod is initially placed so that one end is 0° C and the other end is 100° C. It is allowed to come to a steady-state temperature distribution. Find this temperature distribution, $u_e(x)$.

b. At time t=0, the one-dimensional rod from Part a is insulated on both ends. This implies that the rod satisfies the PDE:

where $u_e(x)$ is the steady state temperature distribution from Part a. Find the solution to this problem, including the Fourier coefficients. Create a graphic simulation showing the 3D plot of temperature as a function of t and x, using 20 and 200 terms (Fourier coefficients) to approximate the solution with $t \in [0, 20]$.