

1. a. The best straight line fit found by Trendline for the Lineweaver-Burk plot with $x = 1/[S]$ and $y = 1/R([S])$ is

$$y = 23.005x + 0.2343.$$

Thus, the value of $1/V_{max} = 0.2343$, and the slope gives $K_m/V_{max} = 23.005$. It follows that $V_{max} = 4.268$ and $K_m = 98.186$. This method for finding the parameters for this experiment on cytochrome P450 mediated demethylation of the substrate $[S]$ amitriptyline (AMI) to nortriptyline (N) by human liver microsomes gives a Michaelis-Menten reaction rate of

$$R([S]) = \frac{4.268[S]}{98.186 + [S]}.$$

b. The Michaelis-Menten model above with the parameters found from the Lineweaver-Burk best fitting line has $[S]$ and R -intercepts of $(0, 0)$ (as is true of all Michaelis-Menten reaction kinetic models). There is a horizontal asymptote of $R = 4.268$, which clearly appears high from the experimental data. Below is a table of the data, the model prediction, and the percent error at various concentrations of $[AMI]$. There is a graph of this model and the one found in the next part at the end of the solutions to this problem.

| $[AMI]$ (μM) | N formation nmol/min/mg | MM Model | % Error |
|---------------------------|----------------------------|----------|---------|
| 15 | 0.6 | 0.5656 | -5.73 |
| 50 | 1.35 | 1.4401 | 6.67 |
| 100 | 2.17 | 2.1535 | -0.76 |
| 200 | 2.68 | 2.8626 | 6.82 |
| 500 | 3.12 | 3.5675 | 14.34 |

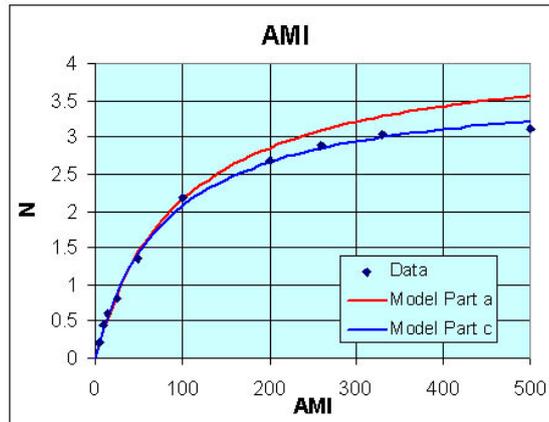
c. With the model

$$R([S]) = \frac{3.738[S]}{80.63 + [S]},$$

the $[S]$ and R -intercepts are $(0, 0)$. There is a horizontal asymptote of $R = 3.738$, which matches the experimental data very well. Below is a table of the data, the model prediction, and the percent error at various concentrations of $[AMI]$. Note that these errors are significantly better than the ones from the Lineweaver-Burk plot.

| $[AMI]$ (μM) | N formation nmol/min/mg | MM Model | % Error |
|---------------------------|----------------------------|----------|---------|
| 15 | 0.6 | 0.5864 | -2.27 |
| 50 | 1.35 | 1.4309 | 5.99 |
| 100 | 2.17 | 2.0696 | -4.63 |
| 200 | 2.68 | 2.6643 | -0.59 |
| 500 | 3.12 | 3.2193 | 3.18 |

Below is a graph of the data and the two models. Clearly the second model is better because it fits the data over the entire range much better.



2. a. Consider the functions,

$$f(x) = x^2 - 3x - 5 \quad \text{and} \quad g(x) = \frac{20x}{1.4 + x}.$$

For $f(x)$, the y -intercept is $(0, -5)$, and the x -intercepts are $(-1.1926, 0)$ and $(4.1926, 0)$. For $g(x)$, the x and y -intercept is $(0, 0)$. The vertex for $f(x)$ is $(1.5, -7.25)$. The function $g(x)$ has a vertical asymptote at $x = -1.4$ and a horizontal asymptote at $y = 20$.

b. There are three points of intersection as can be seen in the graph below. The three points of intersection are $(-4.5189, 28.977)$, $(-0.24347, -4.2103)$, and $(6.3624, 16.393)$.

