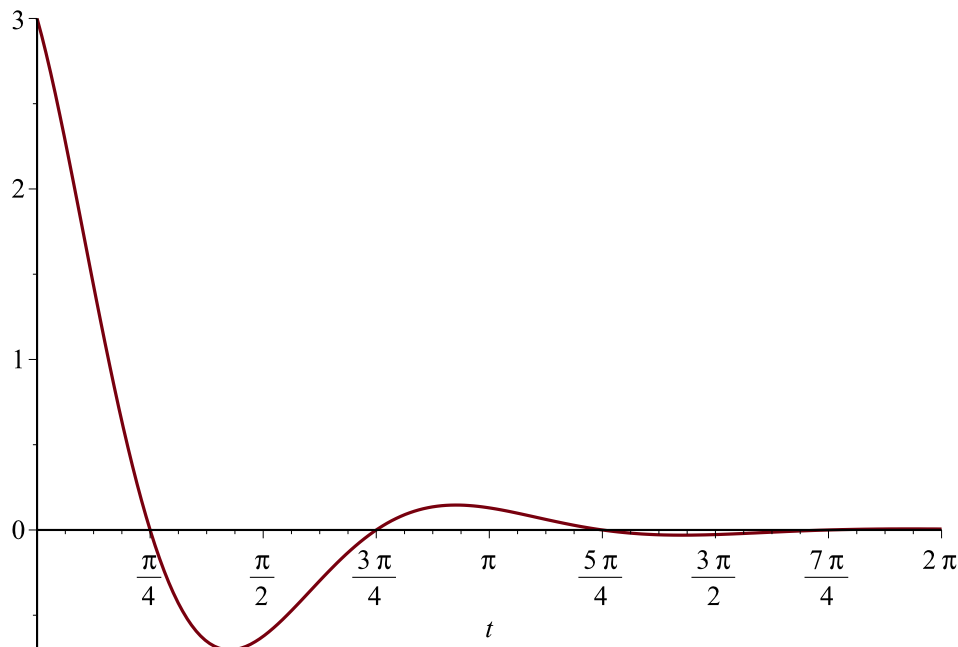


```
> y := t -> 3 * exp(-t) * cos(2*t);    # This enters a function.
      y := t -> 3 e-t cos(2 t)
```

(1)

The arrow is created by typing - and >. The multiplication is *. Exponentiation uses ^. The := in Maple means "defined to be."

```
> plot(y(t), t=0..2*Pi);    # This plots the function
```



```
> dy := diff(y(t), t);    # This differentiates the function
      dy := -3 e-t cos(2 t) - 6 e-t sin(2 t)
```

(2)

Maple stores the derivative of y(t) as dy.

```
> tmin := fsolve(dy=0, t=1..2); y(tmin);    # This finds the minimum
      tmin := 1.338972522
      -0.7033279401
```

(3)

The absolute minimum occurs at (1.33897, -0.703328).
fsolve solves an equation, and here the solution search is restricted between 1 and 2.

```
> tmax := fsolve(dy=0, t=2.5..3.5); y(tmax);    # This finds a local maximum
      tmax := 2.909768849
      0.1462075142
```

(4)

```
> int(y(t), t);    # This finds the indefinite integral
      -\frac{3}{5} e-t cos(2 t) + \frac{6}{5} e-t sin(2 t)
```

(5)

```
> int(y(t), t=0..5); evalf(%);    # This finds the definite integral from 0 to 5
```

$$\frac{3}{5} - \frac{3}{5} e^{-5} \cos(10) + \frac{6}{5} e^{-5} \sin(10)$$

$$0.5989934692 \quad (6)$$

The evalf function gives decimal values, while % means evaluate the previous expression

```
> sdy := diff(y(t), t$2); # This takes the second derivative of y(t)
```

$$sdy := -9 e^{-t} \cos(2 t) + 12 e^{-t} \sin(2 t) \quad (7)$$

We want to see if y(t) satisfies the differential equation $y'' + 2y' + 5y = 0$.

```
> sdy + 2·dy + 5·y(t);
```

$$0 \quad (8)$$

```
> de := diff(Y(t), t$2) + 2·diff(Y(t), t) + 5·Y(t) = 0;
```

$$de := \frac{d^2}{dt^2} Y(t) + 2 \left(\frac{d}{dt} Y(t) \right) + 5 Y(t) = 0 \quad (9)$$

```
> dsolve(de, Y(t)); # This solves the differential equation
```

$$Y(t) = _C1 e^{-t} \sin(2 t) + _C2 e^{-t} \cos(2 t) \quad (10)$$

```
> dsolve( {de, Y(0) = 2, D(Y) (0) = -1 }, Y(t)); # This solves the initial value problem
```

$$Y(t) = \frac{1}{2} e^{-t} \sin(2 t) + 2 e^{-t} \cos(2 t) \quad (11)$$

```
> Y := unapply(rhs(%), t); # This transforms the solution into the function Y(t)
```

$$Y := t \rightarrow \frac{1}{2} e^{-t} \sin(2 t) + 2 e^{-t} \cos(2 t) \quad (12)$$

```
> plot(Y(t), t = 0 .. 2·Pi);
```

