

1. (1 pt) mathbioLibrary/setABiocLabs/Lab121.D3.dog.study.pg

Because of the accuracy of WebWork, you should use 5 or 6 significant figures on all problems.

A collection of dogs were measured and weighed producing the following table of data [1]. (Note that the length is from nose to anus.)

Length (cm)	Body Weight (gm)	Surface Area (cm <sup>2</sup> )
50	3520	2290
61	5270	3185
73	5520	3700
78	10240	5150
97	17220	8080
100	26320	8930
105	33250	10720

a. The first model examines Weight,  $w$ , as a function of the Length,  $u$ . Use Excel's Trendline with the Power law to find the best fit to the data for a model of the form:

$$w = ku^a.$$

The best fit coefficients,  $k$  and  $a$ , found by Excel are

$$k = \underline{\hspace{2cm}}.$$

$$a = \underline{\hspace{2cm}}.$$

Determine the sum of square errors between the weight model and the data.

$$\text{Sum of Square Errors} = \underline{\hspace{2cm}}.$$

If we assume that this model gives the ideal weight for a dog, then a dog with a length of 73 cm should weigh

$$\text{Weight of 73 cm dog} = \underline{\hspace{2cm}} \text{ gm}.$$

Assuming this model gives the best value, compute the percent error that the 73 cm dog in the table varies from the ideal dog in weight.

$$\text{Percent Error (weight) for 73 cm dog} = \underline{\hspace{2cm}}.$$

Suppose a dog has a length of 100 cm, then according to the model should weigh

$$\text{Weight of 100 cm dog} = \underline{\hspace{2cm}} \text{ gm}.$$

Again, assuming this model gives the best value, compute the percent error that the 100 cm dog in the table varies from the ideal dog in weight.

$$\text{Percent Error (weight) for 100 cm dog} = \underline{\hspace{2cm}}.$$

Suppose you have a dog that weighs 13320 gm. According to the model, what would you predict would be its length?

$$\text{Length of 13320 gm dog} = \underline{\hspace{2cm}} \text{ cm}.$$

b. In your Lab report create a plot of this best fitting curve with the data. What are the appropriate units for the coefficient  $k$ ? Write a brief paragraph to explain why the coefficient  $a$  has the value it does when fitting the weight data for the dogs.

c. Repeat the process in Part a for the surface area data,  $s$ , as a function of length,  $u$ . In this case the model satisfies the allometric model:

$$s = ku^a,$$

where the coefficients  $k$  and  $a$  differ from Part a. The best fit coefficients,  $k$  and  $a$ , found by Excel are

$$k = \underline{\hspace{2cm}}.$$

$$a = \underline{\hspace{2cm}}.$$

Determine the sum of square errors between the surface area model and the data.

$$\text{Sum of Square Errors} = \underline{\hspace{2cm}}.$$

If we assume that this model gives the ideal surface area for a dog, then a dog with a length of 73 cm should have a surface area

$$\text{Surface area of 73 cm dog} = \underline{\hspace{2cm}} \text{ cm}^2$$

Assuming this model gives the best value, compute the percent error that the 73 cm dog in the table varies from the ideal dog in surface area.

$$\text{Percent Error (surface area) for 73 cm dog} = \underline{\hspace{2cm}}.$$

Suppose a dog has a length of 100 cm, then according to the model should have a surface area

$$\text{Surface area of 100 cm dog} = \underline{\hspace{2cm}} \text{ cm}^2.$$

Again, assuming this model gives the best value, compute the percent error that the 100 cm dog in the table varies from the ideal dog in surface area.

$$\text{Percent Error (surface area) for 100 cm dog} = \underline{\hspace{2cm}}.$$

Suppose you have a dog that has a surface area 6765 cm<sup>2</sup>. According to the model, what would you predict would be its length?

$$\text{Length of 6765 cm}^2 \text{ dog} = \underline{\hspace{2cm}} \text{ cm}.$$

d. In your Lab report create a plot of this best fitting curve with the data. What are the appropriate units for the coefficient  $k$ ? Write a brief paragraph to explain why the coefficient  $a$  has the value it does when fitting the surface area data for the dogs.

[1] J. Mazumdar (1989), An Introduction to Mathematical Physiology and Biology, Australian Mathematical Society Lecture Note Series, Cambridge University Press, Cambridge.